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# A Gaussian Leftover Hash Lemma for Modules over Number Fields

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## Résumé

Given a Gaussian matrix  $X$ , a Gaussian Leftover Hash Lemma (LHL) states that  $X^*v$  for a Gaussian  $v$  is an essentially independent Gaussian sample. It has seen numerous applications in cryptography for hiding sensitive distributions of  $v$ . We generalise the Gaussian LHL initially stated over  $\mathbb{Z}\mathbb{Z}$  by Agrawal, Gentry, Halevi, and Sahai (2013) to modules over number fields. Our results have a sub-linear dependency on the degree of the number field and require only polynomial norm growth:  $\|v\|/\|X\|$ . To this end, we also prove when  $X$  is surjective (assuming the Generalised Riemann Hypothesis) and give bounds on the smoothing parameter of the kernel of  $X$ . We also establish when the resulting distribution is independent of the geometry of  $X$  and establish the hardness of the  $k$ -SIS and  $k$ -LWE problems over modules based on the hardness of SIS and LWE over modules, which was assumed without proof in prior works.

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